University of California at San Diego – Department of Physics – Prof. John McGreevy Physics 211C (239) Phases of Quantum Matter, Spring 2021 Assignment 5

Due 12:30pm Monday, May 10, 2021

Thanks for following the submission guidelines on hw01. Please ask me by email if you have any trouble.

1. Quasiparticle wavefunctions.

- (a) Use the parton construction of the Laughlin ν = 1/m state to construct wavefunctions for the quasihole and quasiparticle.
 (Hint: add or remove a single parton. Don't forget to project onto the lowest Landau level.)
- (b) Construct a wavefunction with *two* quasiholes and use it to verify their statistics.
- 2. Hall plateaux as a crazy manifestation of quantum oscillations. Check the claim that the hierarchy states at fillings $\nu = \frac{\nu^*}{2\nu^* \pm 1}$ for $\nu^* \in \mathbb{Z}$ can be regarded as an extreme version of quantum oscillations in the HLR state at $\nu = \frac{1}{2}$.
- 3. Charges of quasiparticles in abelian CS EFT.

In an abelian CS theory with K-matrix K, show that a quasiparticle with charge ℓ^{I} under CS gauge field a^{I} has electric charge

$$q_l = tK^{-1}l.$$

4. Excitations of hierarchy states. Find the torus groundstate degeneracy, and the charges and statistics of the quasiparticle excitations of the abelian incompressible FQH state at $\nu = \frac{2}{5}$.